



Highly enantioselective carbene-catalyzed δ -lactonization *via* radical relay cross-coupling

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ABSTRACT

An *N*-heterocyclic carbene (NHC) catalyzed enantioselective cyclisation and trifluoromethylation of olefins with cinnamaldehydes *via* radical relay cross-coupling in the presence of Togni reagent is reported and δ -lactones tolerated with stereogenic centers at β - and γ -positions are obtained in moderate to high yields and with high enantioselectivities. Further computational studies explain that the radical cross-coupling step is the key to determining the enantioselectivity. Energy analysis of key transition states and intermediates also provides a reasonable explanation for the difficulty of diastereoselective control. DFT calculations also reveal that the hydrogen-bonding interaction plays a vital role in the promotion of this chemistry.

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Over the past decades, *N*-heterocyclic carbenes (NHCs) have emerged as a powerful tool for synthetic reactions, medicinal skeletons and their biological functions [1–24]. Its catalytic abilities of HOMO or LUMO activation of aldehydes or carboxylic acids have been extensively studied [25–27]. Although the single-electron transfer capacity of carbene intermediates was predicted in the 1990s [28,29], there are extremely limited examples of NHC-catalyzed radical reactions [10,13]. The pioneering work of carbene-catalyzed radical reaction was reported by Studer and co-workers in 2008 [30]. Since then, this reaction mode has gradually become a hot spot in the field of NHC catalysis [31–34]. Intermediates generated from NHCs and carbonyl compounds can be converted *via* single-electron transfer to generate several new radical species, such as ketyl radical [35–45] and homoenolate radical [46–52]. The reactivity of these radical intermediates has been explored in recent years and used to construct a few important chemical structures [10,13,40,43–45]. Despite these achievements, only limited examples have been reported for NHC-catalyzed asymmetric radical reactions, such as enantioselective β -hydroxylation [46,48], alkylation [47], arylation [52] of enals and asymmetric synthesis of α -substituted ketones [45]. Later on, the cyclization *via* homoenolate radicals has also been achieved. Ye *et al.* accomplished the NHC catalyzed asymmetric [3 + 2] annulation of dioxindoles with enals [49,54]. To date, the enantioselective radical relay couplings

involving the formation of multiple chemical bonds are considered to be one of the most effective methods for delivering complex molecules [53]. Since it does not require the use of stoichiometric oxidants or additives to achieve catalytic cycling, this strategy is considered a practical strategy with atomic economy. To our knowledge, NHC-catalyzed radical relay coupling has been explored to a certain degree. In 2019 [36], the Ohmiya group reported a distinguished SET process between Breslow intermediates and redox-active esters to generate ketyl radical and alkyl radical, thereby completing simple alkyl acylation of styrenes (Scheme 1a, left). Since then, a large number of ketyl radical precursors have been applied to such reactions, resulting in a variety of bifunctional olefins. Moreover, it's associated highly enantioselective versions have rarely been reported. In 2019, the Li group achieved acylfluoroalkylation of olefins by ketone radical relay coupling, but its high enantioselectivity synthesis attempt was unsuccessful (20% *ee*) [37]. In 2021, the Huang group disclosed an elegant homoenolate radical relay cross-coupling reaction (Scheme 1a, right), accessing to a broad spectrum of β -substituted linear carboxylic acid derivatives, but also albeit in poor enantioselectivity control (27% *ee*) [51]. Recently, the relay coupling between ketyl radicals and prochiral carbon radicals was attempted by Zhao and coworkers, but the enantioselectivity control of this process remained unresolved (3% *ee*) [40]. It is no doubt that the NHC-catalyzed highly enantioselective radical relay cross-coupling still remains highly elusive.

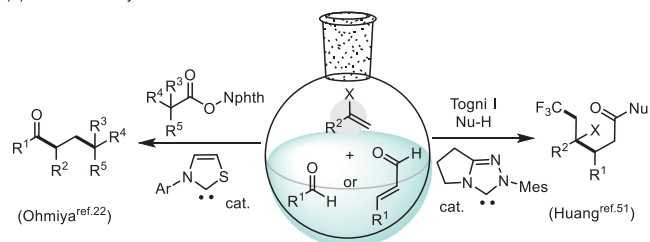
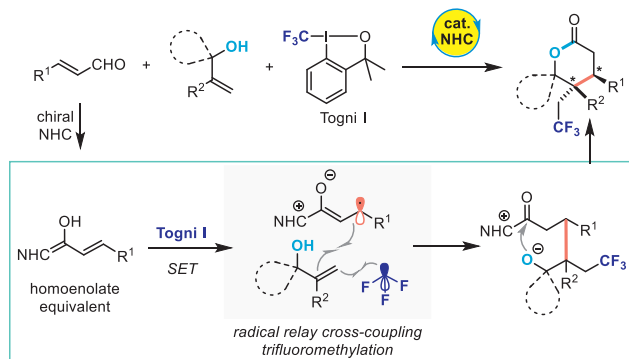
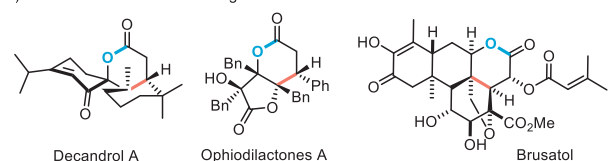
Herein, we reported an NHC-catalyzed highly enantioselective radical relay cross-coupling reaction that constructs a spirocyclic

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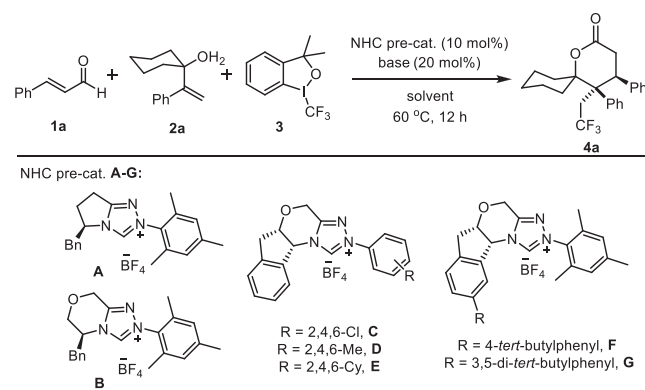
(a) Carbene-catalyzed bisfunctionalization of alkenes

(b) This work: **Highly enantioselective** (up to **99% ee**) carbene-catalyzed δ -lactonization and trifluoromethylation via radical relay cross-coupling (1st example)(c) Bioactive molecules containing δ -lactone with vicinal chiral centers**Scheme 1.** Background of NHC-catalyzed enantioselective radical coupling.

δ -lactone structure with two adjacent chiral centers and also contains a CF_3 fragment (Scheme 1b) [55–57]. It is worth noting that δ -lactones with vicinal chiral centers at β and γ position are a common skeleton in bioactive compounds (Scheme 1c), such as Decandrol A [58,59], Ophiodilactones A [60] and Brusatol [61].

We began our investigation with *trans*-cinnamaldehyde **1a**, 1-(1-phenylvinyl)cyclohexan-1-ol **2a**, and Togni **I** as model substrates. With the NHC pre-catalyst **A**, the desired product **4a** was formed in 30% yield with 1:1 *dr* and moderated *ee* (entry 1). A briefly screen of chiral NHC pre-catalysts indicated that the aminoindanol-derived NHC-pre cat. **D** afforded better yield and enantioselectivity (entry 4). Replacing the *N*-phenyl unit of cat. **C** with electron-withdrawing trichlorophenyl or replacing the *N*-phenyl unit with a bulkier cyclohexyl group reduced enantioselectivity and did not significantly improve yield (entries 4 and 5). Using 4-*tert*-butylphenyl-derived aminoindanol **F** as pre-NHC cat., the *ee* value was increased slightly. To our delight, when introducing 3,5-di-*tert*-butylphenyl group to further increase the bulkiness of aminoindanol scaffold (pre-NHC cat. **G**), excellent enantioselectivity and moderate yield were achieved (entry 10). In addition, highly polar solvent DMF tent to provide better catalytic performance. Exchanged DBU with inorganic base did not offer satisfied results (entries 11 and 12). Finally, adjusting the ratio of substrates **1a** and **2a** afforded product **4a** with 75% yield, 1:1 diastereoselectivity, and excellent *ee* (entry 13).

With the optimal conditions in hand, we investigated the scope by testing various aldehydes. As shown in Table 1, a broad range of aldehydes with diverse electronic properties was well tolerated. When a fluorine located at the 3-position of the phenyl ring (**1b**), a result of 79% yield, *dr* = 1:1, 98% and 90% *ee*, respectively, was observed (**4b**). When methoxy group replaced fluo-

Table 1Optimization of the reaction conditions.^a

Entry	NHC	Solvent	Base	Yield (%) ^b	<i>dr</i> ^c	<i>ee</i> (%) ^d
1	A	MeCN	DBU	30	1:1	–40, –68
2	B	MeCN	DBU	36	1:1.1	–43, –79
3	C	MeCN	DBU	50	1:1.7	70, 81
4	D	MeCN	DBU	53	1:1.5	84, 92
5	E	MeCN	DBU	57	1:1.4	80, 90
6	F	MeCN	DBU	47	1:1	89, 94
7	G	MeCN	DBU	61	1:1.2	92, 96
8	G	THF	DBU	30	1:1.3	92, 98
9	G	DCE	DBU	46	1:1.2	89, 98
10	G	DMF	DBU	68	1:1	93, 99
11	G	DMF	Cs_2CO_3	56	1:1.2	92, 92
12	G	DMF	K_3PO_4	52	1:1	98, 95
13	G	DMF	DBU	80 ^e (75 ^f)	1:1	92, 98

^a Reaction conditions: **1a** (0.10 mmol), **2a** (0.15 mmol), NHC pre-cat. **A-G** (0.01 mmol), base (0.02 mmol), **3** (0.15 mmol) were stirred in solvent (1 mL) at 60 °C under nitrogen for 12 h.

^b Yields were determined by ¹⁹F NMR analysis.

^c *dr* was determined by ¹⁹F NMR analysis.

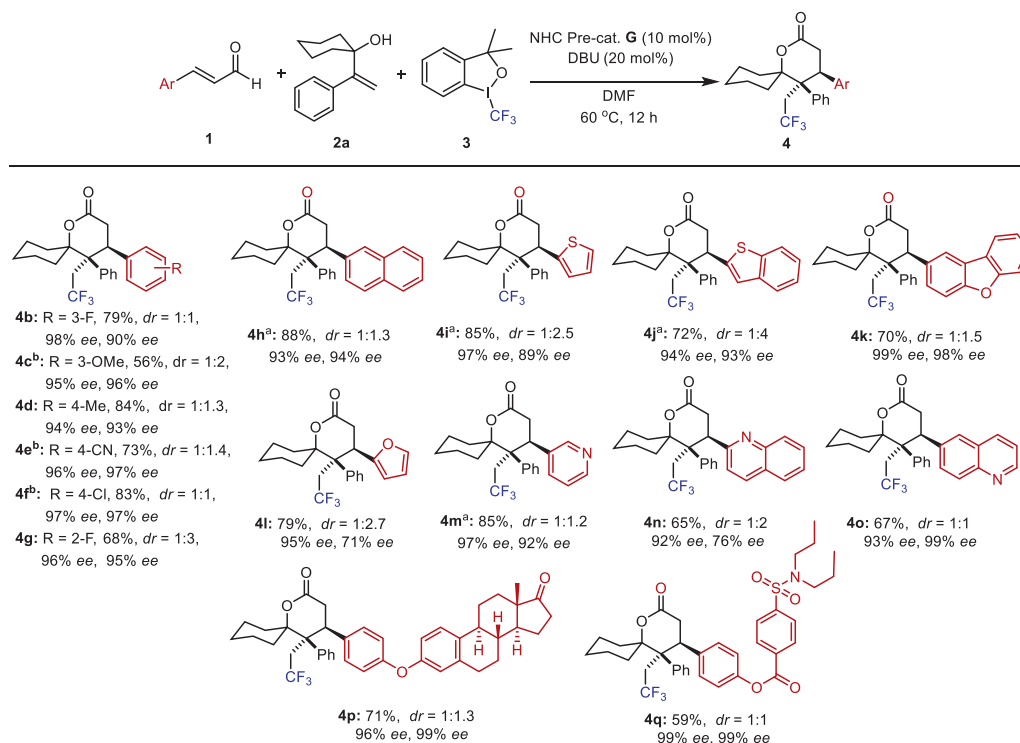
^d Enantiomeric ratios were determined by HPLC.

^e **1a** (0.15 mmol), **2a** (0.10 mmol).

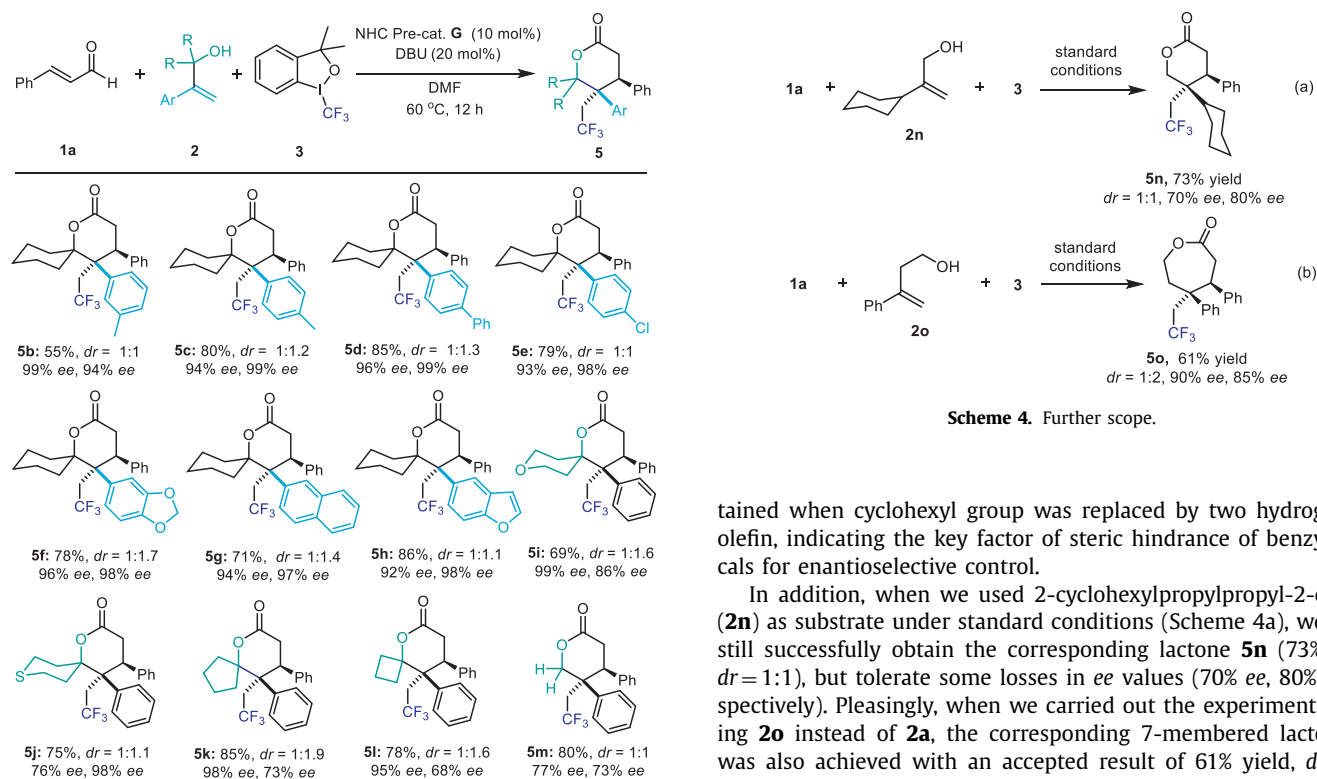
^f Isolated yield.

rine, a good yield and an excellent *ee* value were achieved (**4c**). Functional groups (e.g., methyl (**4d**), cyano (**4e**), chlorine (**4f**)) located at the 4-position were all well tolerated. When a fluorine located at the 2-position of the phenyl ring, a result of 68% yield, *dr* = 1:3, 98% and 95% *ee*, respectively, was observed (**4g**). Substrates bearing with (hetero)cycles, such as 2-naphthyl, 2-thienyl, 2-benzothiophenyl, 2-dibenzofuranly, 2-furanyl, 3-pyridyl, 2-quinolinyl, 6-quinoline group, all afforded their corresponding chiral lactones (**4h–4o**) in moderate to high yields, 1:1 to 1:4 *dr* and with excellent *ee* values. Notably, the estrone and probenecid derived aldehydes had proved to be compatible with this system (**4p** and **4q**). The absolute configurations of two diastereoisomers ((4*S*,5*S*)-**4f** (CCDC: 2303772) and ((4*S*,5*R*)-**4f** (CCDC: 2303773)) were determined by X-ray crystallography (Scheme 2), and other products were assigned by analogy.

Next, we turned our attention to investigate the scope of alkenes (Scheme 3). *meta*-Substituted olefin afforded the product **5b** in a 55% yield with a high *ee* value. The electronic properties of aryl substituents had little effect on chemical yields (**5c–5e**). Unfortunately, *ortho*-substituted olefins exhibit a lower conversion rate in the reaction, possibly because the radical intermediate formation is impeded, which greatly reduces the efficiency of the critical coupling step. Disubstituted styrene (**5f**) and naphthyl styrene (**5g**) were tolerable in our protocol. Heteroaryl olefin also gave the desired adduct in good yield and high *ee* value (**5h**). Then, we explored the impact of R group on substrate **2**. When tetrahydro-2*H*-pyranyl and tetrahydro-2*H*-thiopyranyl were used, both good yields and high to excellent enantioselectivities were achieved (**5i** and **5j**).



Scheme 2. Scope of cinnamaldehyde **1**. Reaction conditions: **1** (0.1 mmol), **2a** (0.15 mmol), NHC pre-cat. **G** (0.01 mmol), DBU (0.02 mmol), **3** (0.15 mmol) were stirred in DMF (1 mL) at 60 °C under nitrogen for 12 h. *dr* was determined by ¹⁹F NMR analysis. ^a MeCN as solvent.



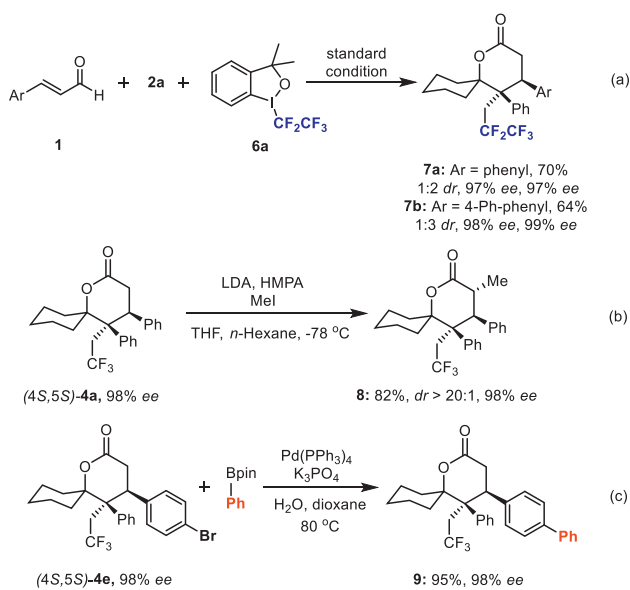
Scheme 4. Further scope.

tained when cyclohexyl group was replaced by two hydrogens in olefin, indicating the key factor of steric hindrance of benzyl radicals for enantioselective control.

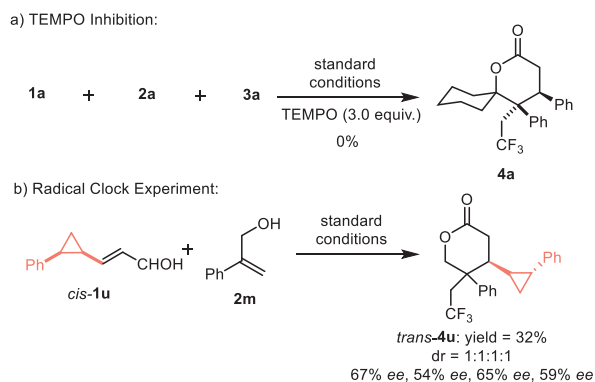
In addition, when we used 2-cyclohexylpropyl-2-en-1-ol (**2n**) as substrate under standard conditions (Scheme 4a), we could still successfully obtain the corresponding lactone **5n** (73% yield, *dr* = 1:1), but tolerate some losses in *ee* values (70% *ee*, 80% *ee*, respectively). Pleasingly, when we carried out the experiment by using **2o** instead of **2a**, the corresponding 7-membered lactone **5o** was also achieved with an accepted result of 61% yield, *dr* = 1:2, 90% and 85% *ee*, respectively.

To further demonstrate the practicality and versatility of this method, we next replaced the trifluoromethyl group with pentafluoroethyl substituent in Togni reagent (**6a**), and the result showed that the reaction could still be well conducted under standard conditions (Scheme 5a). Methylation at α position of carbonyl group of isomer (4*S*,5*S*)-**4a** yielded the corresponding product **8** in good yield and excellent stereoselectivity (Scheme 5b). (4*S*,5*S*)-**4e** was

Then, we varied the ring sizes. Decreased *ee* values of one obtained isomer were observed (**5k** and **5l**, 80% *ee* and 70% *ee*, respectively). Additionally, only moderate *ee*'s for both isomers (**5m**) were ob-



Scheme 5. Further transformations.



Scheme 6. Mechanistic studies.

successfully and equivalently converted to biphenyl compound **9** by Suzuki coupling reaction (Scheme 5c).

To verify the mechanism, several experiments were carried out. As shown in Scheme 6a, 2,2,6,6-tetramethylpiperidinyloxy (TEMPO) effectively inhibited the occurrence of the reaction, suggesting that the reaction may be a radical pathway. In addition, the radical clock experiment with *cis*-**1u** as substrate generated *trans*-lactone, which suggested the ring opening and closing processes of cyclopropane, and the results were consistent with these reported by the Huang group (Scheme 6b).

DFT calculations were performed to further deepen the understanding of the reaction mechanism, including enantioselective and diastereoselective control (For details, see Supporting information). Coupling process between **Int3** (homoenolate radical) and **Int4** (benzyl radical) is a critical step in determining enantioselectivity. Both **Int3** and **Int4** have *Re* and *Si* faces, so there are four coupling modes. The calculation shows that the energy barriers of **TS3** (**Int3** *Si*, **Int4** *Si*, $\Delta G^\ddagger = 5.6$ kcal/mol) lead to (*S,S*)-product) and **TS4** (**Int3** *Si*, **Int4** *Re*, $\Delta G^\ddagger = 5.7$ kcal/mol) lead to (*S,R*)-product) are very low and close to each other, while **TS5** (**Int3** *Re*, **Int4** *Re*, $\Delta G^\ddagger = 17.1$ kcal/mol) lead to (*R,R*)-product) and **TS6** (**Int3** *Re*, **Int4** *Si*, $\Delta G^\ddagger = 14.5$ kcal/mol) lead to (*R,S*)-product) have much higher barriers, indicating that the reaction will not proceed in these two ways.

How to explain the low diastereoselectivity observed in the experiment? The DFT calculation results (Fig. S1 in Supporting in-

formation) show that the difference in energy barrier between the *Re* and *Si* faces of **Int4** is basically negligible, so **Int3** can react with **Int4** from two faces almost equally. This results in the energies of **TS3** and **TS4** being very close and produces **4a** and **4a'** in an almost 1:1 ratio. DFT calculations are completely consistent with the observed low diastereoselectivity. All the calculations were done at the level of SMD [62]-(DMF)-(U)-M06-2X [63]-D3 [64]/def2-TZVPP//def2-SVP [65]. Lu's Multiwfn [66] software is used for wavefunction analysis. RDG plots [67] were drawn to display the noncovalent interactions in the transition state (Fig. S2 in Supporting information). Meanwhile, DIAS [68] analyses were also carried out to give insights on the deformation of fragments and interaction between them.

In summary, we have developed an *N*-heterocyclic carbene (NHC) catalyzed highly enantioselective cyclisation and trifluoromethylation of olefins with cinnamaldehydes via radical relay cross-coupling in the presence of Togni reagent, providing poly-substituted δ -lactones bearing with two adjacent stereogenic centers at β - and γ -positions in good to high yields, moderate diastereoselectivities, and high to excellent enantioselectivities. Further computational studies explain that the radical cross-coupling step is the key to determining the enantioselectivity. DFT calculations also reveal that the hydrogen-bonding interaction plays a vital role in the promotion of this chemistry. Further investigations on novel radical relay cross-couplings catalyzed by NHCs are ongoing in our laboratory.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Supplementary materials

Supplementary material associated with this article can be found, in the online version, at doi:10.1016/j.ccl.2024.109790.

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