



## A comparative study on the reactivity of cationic niobium clusters with nitrogen and oxygen

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### ABSTRACT

We have prepared well-resolved  $\text{Nb}_n^+$  ( $n = 1-10$ ) clusters and report here an in-depth study on the essentially different reactivity with  $\text{N}_2$  and  $\text{O}_2$ , by utilizing a multiple-ion laminar flow tube reactor in tandem with a customized triple quadrupole mass spectrometer (MIFT-TQMS). As results, the  $\text{Nb}_n^+$  clusters are found to readily react with  $\text{N}_2$  and form adsorption products  $\text{Nb}_n\text{N}_{2m}^+$ ; in contrast, the reactions with  $\text{O}_2$  give rise to  $\text{Nb}_n\text{O}_{1-4}^+$  products, and the odd-oxygen products indicate O-O bond dissociation, as well as increased mass abundance of  $\text{NbO}^+$  pertaining to oxygen-etching reactions. We illustrate how  $\text{N}_2$  prefers a physical adsorption on  $\text{Nb}_n^+$  clusters with an end-on orientation for all the products, and allow for size-selective  $\text{Nb}_n^+$  clusters to act as electron donor or acceptor in forming  $\text{Nb}_n\text{N}_{2m}^+$ . In contrast to these nitrides, the dioxides  $\text{Nb}_n\text{O}_2^+$  display much larger binding energies, with  $\text{O}_2$  always as an electron acceptor, corresponding to superoxide or peroxide states in the initial reactions. Density-of-states and orbital analyses show that the interactions between  $\text{Nb}_n^+$  and  $\text{O}_2$  are dominated by strong  $\pi$ -backdonation indicative of incidental electron transfer; whereas weak  $\pi$ -backdonation and simultaneous  $\sigma$  donation interactions exist in  $\text{Nb}_n\text{N}_2^+$ . Further, reaction dynamics analysis illustrates the different interactions for  $\text{N}_2$  and  $\text{O}_2$  in approaching the  $\text{Nb}_n^+$  clusters, showing the energy diagrams for  $\text{N}_2$  adsorption and O-O bond dissociation in producing odd-oxygen products. Fragment analyses with orbital correlation and donor-acceptor charge transfer are also performed, giving rise to full insights into the reactivities and interactions of such transition metal clusters with typical diatomic molecules.

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Gas adsorption is one of the most basic interfacial phenomena and closely related to diverse applications in industrial and agricultural production and daily life. People may take it for granted that the adsorption of gas molecules on the metals is simply divided into physical adsorption and chemical adsorption; however, the underlying mechanism that determines the diverse interactions and surface reactivity at reduced sizes are illusive to be fully understood. The study of gas adsorption on solid surfaces is helpful to understand the micro-mechanism of various physicochemical processes; also, adsorption of gas molecules on nanometals is a key step in catalytic processes and important for various gas phase reactions. While physisorption is often dominated by molecular van der Waals force and generally emits rare energies, chemisorption can be largely exothermic and may involve covalent interactions and stepwise reactions [1]. In this regard, molecular adsorption

can be associated with three processes, *i.e.*, inactivated adsorption, activated adsorption and precursor-mediated adsorptions [2]. The adsorbate may reach a chemisorption state through a barrierless process directly from physisorption state; or it needs to overcome a potential barrier simply by heating or other reaction conditions; or undergoes a precursor-mediated adsorption, where the chemisorbed state could be attained through a precursor intermediate.

On this basis, the reactivities of transition metal clusters with small molecules have been extensively studied, illustrating the distinction of physical and chemical adsorptions on surfaces [2]. Also, the interaction mechanisms and properties of metal cluster complexes have been widely analyzed by joint experimental and theoretical studies. Among them, niobium clusters have been an important research object unveiling size-dependent chemical and physical properties of transition metals at reduced sizes [3–10]. Combining mass spectrometry and gas flow reactors [11,12], the reac-

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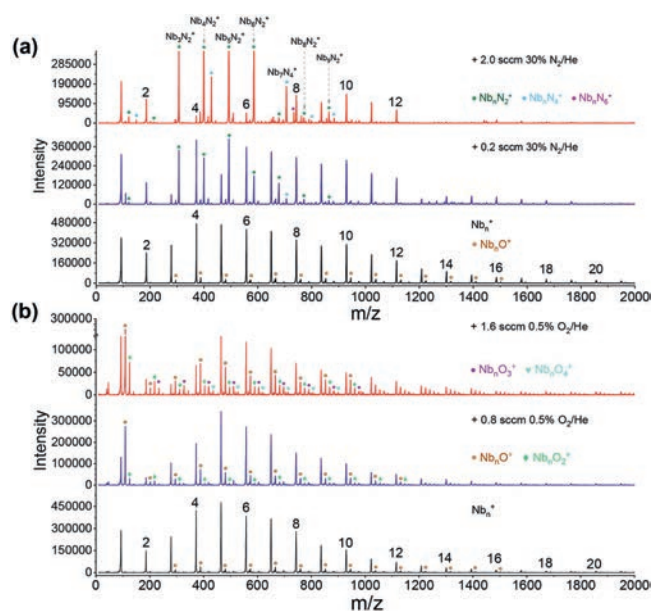
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tivities of niobium clusters with many chemicals have been studied, such as  $H_2$  [12–15],  $O_2$  [16,17],  $N_2$  [18,19],  $CO_x$  [20–22],  $NO_x$  [23,24] and hydrocarbons [25–29]. The reactions of Nb clusters with  $N_2$  and  $H_2$  ( $D_2$ ) have similar adsorptive patterns; while the reaction with  $O_2$  shows a difference due to the differences of atomic valence configuration and bonding nature of these diatomic molecules. In general,  $N_2$  is inert in most reactions due to a very high dissociation energy (945 kcal/mol) of the  $N\equiv N$  triple bond and a high HOMO-LUMO gap ( $\sim 10.82$  eV); in comparison, ground-state  $O_2$  is in triplet with two spin single electrons pertaining to its high activity [30]. However, it is not fully unveiled how the stability of such metal clusters and atomic valence configuration and bonding nature cooperatively determine the experimental observation on their reactivity.

On the other hand, previously published studies have also estimated the reaction rate constants for niobium clusters with  $N_2$  and  $O_2$  showing a likely difference of three orders of magnitude [18,19]. Further studies reported the similar adsorption of  $N_2$  on niobium clusters [18,19,31], and there are adsorption products of polynitrogen molecules depending on the pressure and concentration of the reaction gas at room temperature [32]. For example, Pillai *et al.* [33] generated  $Nb^+(N_2)_n$  complexes ( $n = 3-16$ ) with nitrogen as buffer gas and investigated the vibration in forming such complexes by infrared photodissociation spectroscopy (IRPD), showing a preferred coordination of six ligands. Meanwhile, the reactions of small  $Nb_n^+$  ( $n = 1-3$ ) with  $O_2$  have been studied by Loh *et al.* [16] who measured the cross section as a function of kinetic energy and proposed dissociation pathways and threshold values. It is anticipated that these experimental cluster physics studies of such small Nb clusters can be connected with theoretical energy calculations in determining the thermodynamics and their reaction dynamics in gas phase [34].

On these bases, here we have performed a further in-depth study of the thermalized gas-phase  $Nb_n^+$  ( $n = 1-10$ ) clusters in reacting with sufficient  $N_2$  and  $O_2$  gas in a customized multiple ions laminar flow tube in tandem with triple quadrupole mass spectrometer (MIFT-TQMS). It is found that the  $Nb_n^+$  clusters, produced by the home-made magnetron sputtering (MagS) source, readily react with both  $N_2$  and  $O_2$ , but form different series of products respectively, seen as  $Nb_nN_{2m}^+$  ( $m = 1-3$ ) and  $Nb_nO_x^+$  ( $x = 1-4$ ). Theoretical calculations results reveal that the  $Nb_nN_{2m}^+$  clusters all adopt end-on orientation adsorption for  $N_2$  on  $Nb_n^+$  with much smaller binding energy than that of correlative  $Nb_nO_x^+$  series which correspond to strong hollow-site adsorption allowing for occasional dissociative adsorption. Further, we conducted a comprehensive study thermodynamic energetics, HOMO-LUMO gaps, charge transfer, Wiberg bond index (WBI), density of state (DOS), natural atomic orbital (NAO) and energy decomposition analyses based on natural orbitals for chemical valence (EDA-NOCV). In addition, we carried out potential scan for  $N_2$  and  $O_2$  in approaching an  $Nb_n^+$  cluster until the formation of  $Nb_3N_2^+$  and  $Nb_3O_2^+$ , illustrating how cluster-molecule interactions initiate their reaction. Finally, we explore the reaction pathways of both  $N_2$  and  $O_2$  with  $Nb_3^+$  as a representative, demonstrate the  $N_2$ -adsorption behavior and the reaction dynamics in producing  $Nb_3O_2^+$  from  $O_2$ -adsorption, to dissociative intermediate, and to ultimately exhaust of  $NbO$  ( $/NbO^+$ ).

The experiments in this study are conducted on our customized multi-ions laminar flow tube reactor in tandem with a triple quadrupole mass spectrometer (MIFT-TQMS). A self-designed MagS source with a DC power supply of 5 kW was used to obtain the clean mass distributions of small niobium clusters [35]. A niobium disk (99.95% purity, 50.8 mm diameter, 4 mm thickness) was used as the sputtering target. High-purity helium ( $>99.999\%$ ) and high-purity argon ( $>99.995\%$ ) were used as carrier gas and sputtering work gas, introduced from the rare of the MagS source and the



**Fig. 1.** The mass spectra of  $Nb_n^+$  clusters in the absence and presence of (a) 30%  $N_2/He$  and (b) 0.5%  $O_2/He$ , respectively. The weak mass peaks marked with stars (\*) in the nascent  $Nb_n^+$  cluster distributions correspond to trace amount of oxygen contamination.

magnetron head respectively, with the gas flow rates controlled by two mass flowmeters (Alicat, a range of 0–100 sccm and 0–100 slm, respectively). Typical parameters for the MagS source to produce the niobium clusters with  $n = 1-10$  are: 170 V DC voltage, 4 A current, a background pressure of source chamber at  $\sim 7$  Torr, He carrier gas at  $\sim 12$  slm helium, while Argon is 60–120 sccm. Different concentrations of  $N_2$  and  $O_2$  (*ca.*, 0.5%–30% in He) are injected into the flow tube (60 mm diameter, 1 m long) which is maintained at 0.9 Torr pressure for stable laminar flow and sufficient collisional reaction. The detailed values for these parameters may differ with dependence on the target situation and vacuum status, *etc.*

All the DFT calculations were performed using Gaussian 09 software package [36]. B3LYP exchange-correlation functional was used to optimize the geometric structures of all the niobium clusters and products, the basis sets of LanL2dz was used for Nb with an extra *d* polarization function, while 6–311G(d) for N and O atoms [36,37]. Vibrational frequency calculations were performed for each of the optimized structures and zero-point vibrations were corrected for all the energy calculations. Thermodynamic data, Wiberg bond index (WBI), partial density of states (PDOS), natural atomic orbital (NAO) and electron configuration are analyzed by using the Multiwfn software [38]. The geometric structures, frontier orbitals, charge distributions by natural population analysis (NPA), and the PDOS patterns of the  $Nb_n^+$ ,  $Nb_nN_{2m}^+$ ,  $Nb_nO_x^+$  ( $n = 1-10$ ) are plotted by visual molecular dynamics (VMD) [39]. Energy decomposition analysis was conducted based on natural orbitals for chemical valence (EDA-NOCV), calculated with Amsterdam Density Functional (ADF) program [40,41] at the B3LYP/TZP level of theory.

Fig. 1 presents the mass spectra of the  $Nb_n^+$  ( $n = 1-21$ ) clusters in the absence and presence of  $N_2$  and  $O_2$  gas reactants respectively, where the concentrations and gas flowrates are controlled by a mass flowmeter (ALICAT-LD12). As is shown in Fig. 1a, most of the  $Nb_n^+$  clusters react with  $N_2$  just to form molecular adsorption products  $Nb_nN_{2m}^+$  ( $m = 1-3$ ) with size dependence, which is in contrast to the sequence reactions between  $Nb_n^+$  and  $O_2$  in forming  $Nb_nO_x^+$  ( $x = 1-4$ ). From mass spectra in Fig. 1a and the

**Table 1**

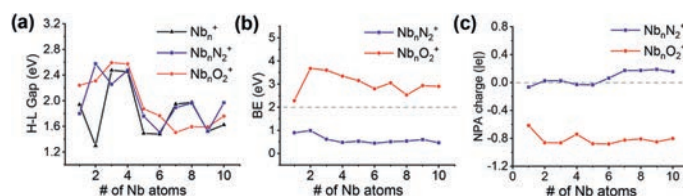
DFT-calculated energies (eV) for the likely diverse reaction pathways of  $\text{Nb}_n^+$  ( $n = 1-10$ ) with  $\text{O}_2$ . All the data are calculated at the B3LYP/Lan12dz level for  $\text{Nb}_n^+$  and B3LYP/6-311G(d) level for N/O.

Reaction channel	1	2	3	4	5	6	7	8	9	10
$\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_n\text{O}_2^+$	-2.28	-3.67	-3.60	-2.77	-3.15	-2.80	-3.05	-2.53	-2.93	-2.90
$\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_{n-1}\text{O}^+ + \text{NbO}$		-5.04	-3.99	-4.54	-4.65	-4.42	-3.99	-3.71	-4.14	-3.13
$\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_{n-1}\text{O} + \text{NbO}^+$		-5.04	-3.60	-2.00	-2.66	-2.31	-1.50	-1.25	-1.60	-1.08
$\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_{n-1}^+ + \text{NbO}_2$		-4.38	-3.35	-2.96	-3.72	-3.54	-2.94	-3.18	-3.68	-3.09
$\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_{n-1} + \text{NbO}_2^+$		-3.08	-1.83	-0.62	-1.04	-0.58	0.10	-0.11	-0.74	0.46
$\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_{n-2}^+ + 2\text{NbO}$			-1.03	0.39	0.02	-0.57	0.22	0.59	-0.15	-0.07
$\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_{n-2}^+ + \text{Nb}_2\text{O}_2$			3.58	5.00	4.62	4.04	4.83	5.19	4.45	4.54
$\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_{n-1}\text{O}_2 + \text{Nb}^+$		0.26	1.41	2.74	2.19	2.57	3.72	3.18	3.06	3.43
$\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_{n-1}\text{O}_2^+ + \text{Nb}$		1.04	0.68	1.14	1.21	1.01	1.97	1.48	1.49	1.68

variation of mass abundances of the nascent  $\text{Nb}_n^+$  clusters and  $\text{Nb}_n\text{N}_2^+$  products (Fig. S1 in Supporting information), it is seen that  $\text{Nb}_{3-6}^+$  clusters react faster than the other clusters and convert to  $\text{Nb}_n\text{N}_2^+$  products. In comparison, the  $\text{Nb}_7^+$  is seen to prefer an adsorption of several nitrogen molecules to form  $\text{Nb}_7\text{N}_{4.6}^+$  (also seen for  $\text{Nb}_4^+$ ); The cation  $\text{Nb}^+$ , also  $\text{Nb}_8^+$  and  $\text{Nb}_9^+$  slowly react with  $\text{N}_2$ , but  $\text{Nb}_2^+$  and  $\text{Nb}_{10}^+$  display rare reaction products with  $\text{N}_2$  in the experimental condition of this study. The variation of  $\text{Nb}_n^+$  clusters reacting with  $\text{N}_2$  reflects their size-dependent stability and reactivity, assuming they undergo identical collision annihilation with the wall of the flow tube. We have plotted the changes in relative intensity of  $\text{Nb}_n^+$  ( $n = 3-9$ ) and  $-\ln(I/I_0)$  of  $\text{Nb}_n^+$  as a function of the gas flow rate (Fig. S3 in Supporting information). The experimental results display that the  $\text{N}_2$  addition on  $\text{Nb}_n^+$  ( $n = 1-10$ ) closely follow the quasi first-order reactions for which the rate constants have been estimated simply by using the equation  $\ln(I_A/I_0) = -k_1(P_e \Delta t / k_B T)$  [42], where  $k_B$  is the Boltzmann constant,  $T$  is the temperature,  $P_e$  and  $\Delta t$  correspond to the effective pressure and reaction time. As results, the size-dependent reaction rates of  $\text{Nb}_n^+$  ( $n = 1-10$ ) exhibit a wide diversity, and  $\text{Nb}_3^+$  is found to display a maximal value of  $\sim 10^{-9} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$ .

There is different case. As shown in Fig. 1b, the  $\text{Nb}_n^+$  ( $n = 1-10$ ) clusters are highly reactive with  $\text{O}_2$  even at a very low concentration (e.g., 0.8 sccm of 0.5%  $\text{O}_2$  in He gas). Even in the presence of a small amount of oxygen, the dissociative products  $\text{Nb}_n\text{O}^+$  are observed. This is reasonable considering the large Nb-O bond energy up to  $\sim 770 \text{ kJ/mol}$  which is even larger than the O-O bond strength ( $\sim 400 \text{ kJ/mol}$ ); and electron transfer readily occur between niobium and oxygen [43,44], with a variety of exothermic reaction channels as given in Table 1. Among the thermodynamically favorable channels, the  $\text{O}_2$ -dissociated equation to produce a NbO neutral suggests the maximal energy release for all the  $\text{Nb}_n^+$  ( $n = 2-10$ ) clusters. This could well explain the experimental observation of dissociative products  $\text{Nb}_n\text{O}^+$  which was also found in previous experimental study [17]. It is worth noting that, such a favorable reaction channel " $\text{Nb}_n^+ + \text{O}_2 \rightarrow \text{Nb}_{n-1}\text{O}^+ + \text{NbO}$ " largely differs from the previously determined reactions of " $\text{Al}_n^+ + \text{O}_2 \rightarrow \text{Al}_m^+ + \text{Al}_{n-m}\text{O}_2$ " [45], " $\text{Al}_n^+ + \text{O}_2 \rightarrow \text{Al}_{n-4}^- + 2\text{Al}_2\text{O}$ " [46] and " $\text{Co}_n^+ + \text{O}_2 \rightarrow \text{Co}_{n-1}^- + \text{CoO}_1^-$ " [47]. Due to the large Nb-O bond energy, here the reaction channels with  $\text{Nb}^{0/+}$  or  $\text{Nb}_2^{0/+}$  removal are much less favorable from the thermodynamics, which is well consistent with the experimental observation that  $\text{Nb}^+$  and  $\text{Nb}_2^+$  do not display increased mass abundance in the varied reaction conditions. Also, this is consistent with the previous study by Radi *et al.* [17], where the dominant reaction pathway of mass-selected small niobium clusters with  $\text{O}_2$  in a drift reactor was proposed to be the one in producing primary products of NbO and  $\text{NbO}^+$ .

Utilizing DFT calculations we have provided further insights into the diverse reactivities of niobium clusters (for details of the lowest-energy structures, spin multiplicity, bond lengths, and point



**Fig. 2.** (a) DFT-calculated HOMO-LUMO gaps of  $\text{Nb}_n^+$ ,  $\text{Nb}_n\text{N}_2^+$  and  $\text{NbO}_2^+$  ( $n = 1-10$ ). (b) Binding energy of  $\text{Nb}_n\text{N}_2^+$  and  $\text{NbO}_2^+$ . (c) NPA charge transfer of  $\text{Nb}_n^+$  to  $\text{N}_2$  in  $\text{Nb}_n\text{N}_2^+$  compared with  $\text{Nb}_n^+$  to  $\text{O}_2$  in  $\text{Nb}_n\text{O}_2^+$ . All the data are calculated at the B3LYP/Lan12dz level for  $\text{Nb}_n^+$  and B3LYP/6-311G(d) level for N/O.

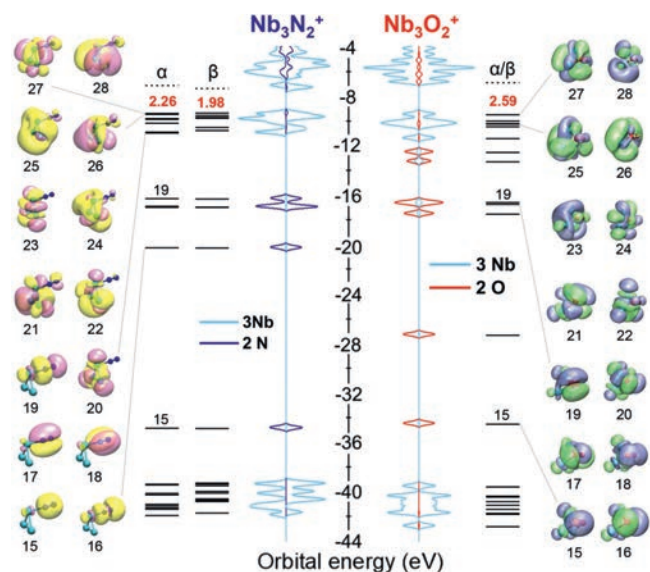
group see Fig. S6 in Supporting information). For the adsorption complexes,  $\text{N}_2$  adopts an end-on adsorption orientation on the  $\text{Nb}_n^+$  clusters of which the nascent structures and spin multiplicities almost do not change, except  $\text{Nb}_2\text{N}_2^+$  which shows a V-shape structure with a high spin multiplicity. In contrast,  $\text{Nb}_n\text{O}_2^+$  ( $n > 2$ ) clusters all adopt hollow-site adsorption mode with elongated O-O bond length ranging from 1.2 Å to 1.5 Å, although the structures of  $\text{Nb}_n^+$  in  $\text{Nb}_n\text{O}_2^+$  do not show such changes. Moreover, the spin multiplicities of the odd-number small niobium clusters (i.e.,  $\text{Nb}_{2n+1}\text{O}_2^+$ ) reduced in the formation of  $\text{Nb}_n\text{O}_2^+$  (except  $\text{Nb}_9\text{O}_2^+$ ); whereas, for the even-number niobium clusters (i.e.,  $\text{Nb}_{2n}^+$ ), the spin of the cluster can be aligned opposite to that of the  $^3\text{O}_2$  molecule thus spin conservation in the  $\text{Nb}_{2n}\text{O}_2^+$  products [48,49].

Fig. 2 plots the DFT-calculated HOMO-LUMO gaps, binding energies (BE), and natural population analysis (NPA) of charge distributions of the  $\text{Nb}_n^+$ ,  $\text{Nb}_n\text{N}_2^+$  and  $\text{NbO}_2^+$  ( $n = 1-10$ ) clusters. More energetics data such as the VSE, ASE, binding energy per atom (BE) and  $\Delta_2E$  of the  $\text{Nb}_n^+$  are given in Fig. S9 (Supporting information). While no surprise that the  $\text{Nb}_n\text{N}_2^+$  clusters show much smaller cluster-molecule binding energies and charge transfer comparing with that of the  $\text{Nb}_n\text{O}_2^+$  products, the HOMO-LUMO gaps of the nascent  $\text{Nb}_n^+$  clusters and the subsequent  $\text{Nb}_n\text{N}_2^+$  and  $\text{Nb}_n\text{O}_2^+$  are comparable with each other except a jump at  $n = 2, 7, 8$  pertaining to altered spin multiplicity ( $\text{Nb}_7\text{O}_2^+$ ), symmetry ( $\text{Nb}_2\text{O}_2^+$ ) or structure changes ( $\text{Nb}_8\text{O}_2^+$ ). Note that,  $\text{O}_2$  always serves as an electron acceptor in interacting with the  $\text{Nb}_n^+$  clusters, with a total electron transfer of 0.6–0.9 |e|, which is in sharp contrast to that of the  $\text{Nb}_n\text{N}_2^+$  complexes of which the  $\sigma$  donations from  $\text{N}\equiv\text{N}$  to the  $\text{Nb}_n^+$  clusters are enabled especially for the larger ones at  $n \geq 6$ . Detailed information about NPA charge and natural electron configuration of  $\text{Nb}_{3/6}^+$ ,  $\text{N}_2$ ,  $\text{O}_2$ ,  $\text{Nb}_{3/6}\text{N}_2^+$  and  $\text{Nb}_{3/6}\text{O}_2^+$  is shown in Tables S3 and S4 (Supporting information).

Table 2 lists the Wiberg bond indexes (WBI) between the atoms in  $\text{Nb}_n\text{N}_2^+$  and  $\text{Nb}_n\text{O}_2^+$  ( $n = 1-10$ ). As is shown, every WBI of the N(1)-N(2) bond in  $\text{Nb}_n\text{N}_2^+$  changes to 2.69–2.90 from the primary  $\text{N}\equiv\text{N}$  triple bond in dinitrogen. Meanwhile, the WBI of the linked N(1)-Nb bond is about 0.3–0.5, while the WBI of N(2)-Nb is as small as 0.05–0.15 indicating weak interaction between the  $\text{Nb}_n^+$  clusters and  $\text{N}_2$  corresponding to physical adsorption. By contrast,

**Table 2**The WBI analysis between the atoms in  $\text{Nb}_n\text{N}_2^+$  and  $\text{Nb}_n\text{O}_2^+$  ( $n = 1-10$ ).

Species		1	2	3	4	5	6	7	8	9	10
$\text{Nb}_n\text{N}_2^+$	N(1)-Nb	0.32	0.30	0.45	0.48	0.46	0.43	0.40	0.43	0.44	0.41
	N(2)-Nb	0.08	0.06	0.11	0.16	0.14	0.10	0.05	0.06	0.06	0.07
	N(1)-N(2)	2.80	2.88	2.81	2.72	2.69	2.81	2.92	2.90	2.89	2.90
$\text{Nb}_n\text{O}_2^+$	O(1)-Nb(1)	1.02	0.48	0.49	0.45	0.51	0.53	0.39	0.34	0.33	0.39
	O(2)-Nb(1)	1.02	0.48	0.49	0.45	0.38	0.35	0.34	0.39	0.33	0.39
	O(1)-Nb(2)	–	0.48	0.43	0.46	0.43	0.33	0.42	0.51	0.47	0.48
	O(2)-Nb(2)	–	0.48	–	–	–	–	–	–	–	–
	O(2)-Nb(3)	–	–	0.42	0.46	0.36	0.45	0.54	0.48	0.47	0.48
	O(1)-O(2)	1.04	1.02	1.02	1.00	1.00	0.95	1.00	0.98	1.00	0.98

**Fig. 3.** Energy level of  $\text{Nb}_3\text{N}_2^+$  and  $\text{Nb}_3\text{O}_2^+$  together with PDOS of 2 N atoms and 3 Nb atoms in  $\text{Nb}_3\text{N}_2^+$  and PDOS of 2 O atoms and 3 Nb atoms in  $\text{Nb}_3\text{O}_2^+$ . Insets show the corresponding orbitals.

every WBI of O-O bond changes to about 1 from O=O double bond in the ground state oxygen molecule, and the bond length elongated from 1.2 Å to 1.4–1.5 Å, which is similar to O-O bond length and bonding mode in  $\text{H}_2\text{O}_2$ , as named peroxy bond (or peroxide state) after a chemical adsorption. Moreover, every O atom links to 2 Nb atoms in the 3Nb-2O elementary units when  $n \geq 3$ , showing two types of O–Nb bonds with a minor different WBI, that is, O(1)–Nb(1,2) and O(2)–Nb(1,3) bond. It is notable that  $\text{Nb}_2\text{O}_2^+$  possesses 4 equal Nb–O bonds (WBI = 0.48) and the WBI of O–O bond is 1.02. In all, the WBI of every Nb–N and Nb–O provides detailed information of their bonding strengths.

We have conducted orbital analysis to reveal the essential interaction of  $\text{Nb}_n^+$  with  $\text{N}_2$  and  $\text{O}_2$ . Fig. 3 presents a comparison for the partial density of states (PDOS) and corresponding orbitals of 2 N(O) atoms and linked 3 Nb atoms typically in  $\text{Nb}_3\text{N}_2^+$  and  $\text{Nb}_3\text{O}_2^+$  respectively. Firstly, the overlap area in PDOS of  $\text{Nb}_3\text{O}_2^+$  is much more than  $\text{Nb}_3\text{N}_2^+$ . For  $\text{Nb}_3\text{N}_2^+$ , this is displayed by the reconstituted  $\text{Nb}_3\text{N}_2^+$  orbital which possesses a pattern involving both the cluster and nitrogen molecule. The PDOS of non-dissociative adsorption of  $\text{N}_2$  gives rise to be seen as  $\sigma_{2s}$ ,  $\sigma_{2s}^*$ ,  $\sigma_{2pz}$  which are associated with the dominant  $\text{N}_2 \rightarrow \text{Nb}_3^+$   $\sigma$  donation interactions, and two equivalent orbitals  $\pi_{2px}$  and  $\pi_{2py}$  involving very few interactions, vacant  $\pi_{2px}^*$  and  $\pi_{2py}^*$  of nitrogen are associated with the  $\text{Nb}_3^+ \rightarrow \text{N}_2$   $\pi$  backdonation interactions (detailed orbital information including the natural atomic orbital (NAO) contributions is seen in Table S5 in Supporting information) [50]. While in  $\text{Nb}_3\text{O}_2^+$ , the interacting orbitals also possess character of free  $\text{O}_2$  molecule, where corre-

sponding to  $\sigma_{2s}$ ,  $\sigma_{2s}^*$ ,  $\sigma_{2pz}$  of oxygen refer to  $\text{O}_2 \rightarrow \text{Nb}_3^+$   $\sigma$  donation, and two equivalent orbital  $\pi_{2px}$  and  $\pi_{2py}$  both contribute to the  $\text{O}_2 \rightarrow \text{Nb}_3^+$   $\pi$  donation interaction; meanwhile, the strong DOS correlative to  $\pi_{2px}^*$  and  $\pi_{2py}^*$  of oxygen accounts for the  $\text{Nb}_3^+ \rightarrow \text{O}_2$  dominant  $\pi$  backdonation (Table S5) [51]. Similarly, the NAO analyses for  $\text{Nb}_6\text{N}_2^+$  and  $\text{Nb}_6\text{O}_2^+$  are given in Table S6 (Supporting information).

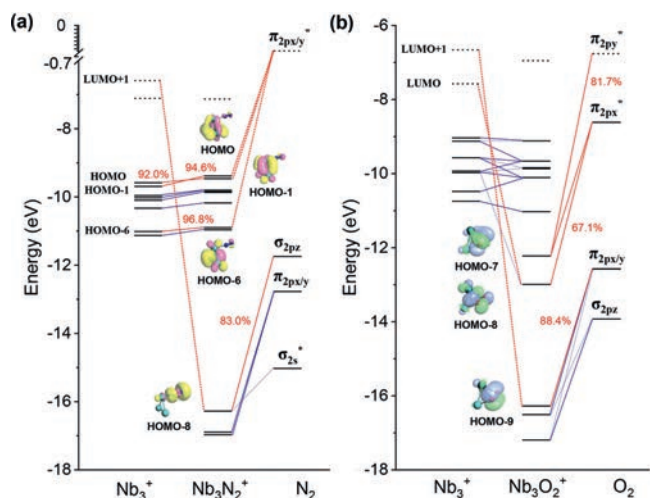
Further, we conducted energy decomposition analysis based on natural orbitals for chemical valence (EDA-NOCV) [52–55]. The typical results of  $\text{Nb}_3\text{N}_2^+$  and  $\text{Nb}_3\text{O}_2^+$  are shown in Table 3, where the strength of the intrinsic interaction energies ( $\Delta E_{\text{int}}$ ) are divided into three components ( $\Delta E_{\text{int}} = \Delta E_{\text{pauli}} + \Delta E_{\text{elstat}} + \Delta E_{\text{orb}}$ ) corresponding to pauli exclusion ( $\Delta E_{\text{pauli}}$ ), electrostatic interaction ( $\Delta E_{\text{elstat}}$ ) and orbital interaction ( $\Delta E_{\text{orb}}$ ) which can be further divided into  $\sigma$  donation,  $\pi$  donation,  $\pi$  backdonation, polarization and the rest interactions. For  $\text{Nb}_3\text{N}_2^+$ ,  $\Delta E_{\text{elstat}}$  and  $\Delta E_{\text{orb}}$  each contributes a half of the attractive interactions; while in  $\text{Nb}_3\text{O}_2^+$ , the  $\Delta E_{\text{orb}}$  contributes about 60%. In total orbital interactions, the  $\text{N}_2 \rightarrow \text{Nb}_3^+$   $\sigma$  donation interaction and polarization interaction contribute ~48%;  $\text{Nb}_3^+ \rightarrow \text{N}_2$   $\pi$  backdonation contributes ~40%. In contrast for  $\text{Nb}_3\text{O}_2^+$ ,  $\Delta E_{\text{orb}}$  is much larger than  $\Delta E_{\text{elstat}}$  in total interactions, among which and the two  $\text{O}_2 \rightarrow \text{Nb}_3^+$   $\pi$  donation interactions contribute only ~13%, reversely,  $\text{Nb}_3^+ \rightarrow \text{O}_2$   $\pi$  backdonation contributes ~83% of the interactions. It is worth mentioning that the interacting fragments  $^3\text{Nb}_3^+$  and  $^3\text{O}_2$  are both in spin triplet, but  $^1\text{Nb}_3\text{O}_2^+$  in singlet state, which results in a larger value of  $\Delta E_{\text{int}}$  than the BE in forming  $\text{Nb}_3\text{O}_2^+$  because of the differences between the unactivated fragments and the activated complex (which involves an additional energy to activate the precursor).

Fig. 4 displays the principal orbitals correlation diagrams of  $\text{Nb}_3\text{N}_2^+$  and  $\text{Nb}_3\text{O}_2^+$  based on the corresponding fragments, with only  $\alpha$ -orbitals being shown as the correlation of  $\beta$ -orbitals is similar. In  $\text{Nb}_3\text{N}_2^+$  (Fig. 4a),  $\text{N}_2 \rightarrow \text{Nb}_3^+$   $\sigma$  donation interaction dominantly forms compound orbital HOMO-8, which is mainly contributed (about 83%) by HOMO of  $\text{N}_2$  ( $\sigma_{2pz}$ ) and vacant LUMO+1 orbital of  $\text{Nb}_3^+$ ; and  $\text{Nb}_3^+ \rightarrow \text{N}_2$   $\pi$  backdonation forms new compound orbitals (HOMO, HOMO-1, HOMO-6) which are composed by the occupied orbitals of  $\text{Nb}_3^+$  and LUMO of  $\text{N}_2$  ( $\pi_{2px/y}^*$ ). In  $\text{Nb}_3\text{O}_2^+$  as a comparison (Fig. 4b), two  $\text{O}_2 \rightarrow \text{Nb}_3^+$   $\pi$  donation interactions form HOMO-8, HOMO-9 orbitals of the complex, which are mainly from the occupied antibonding HOMO ( $\pi_{2px}^*$ ) and one of the degenerate orbitals ( $\pi_{2py}$ ) of  $\text{O}_2$ , coupled with vacant orbitals (LUMO, LUMO+1) of  $\text{Nb}_3^+$ . Here  $\pi$  backdonation interactions sourcing from bonding orbitals of  $\text{Nb}_3^+$  and LUMO ( $\pi_{2py}^*$ ) of  $\text{O}_2$  ( $\text{Nb}_3^+ \rightarrow \text{O}_2$ ) play a dominant contribution and form HOMO-7 orbital of the  $\text{Nb}_3\text{O}_2^+$  complex. The electrons on  $\text{O}_2$  fragment  $\pi_{2py}^*$  orbital (Fig. S14 in Supporting information) stem from charge transfer and orbital interactions [56,57]. In addition, NOCV analysis including detailed values of interaction energies and the shapes of electron deformation densities ( $\Delta\rho$ ) are shown in Figs. S17 and S18 (Supporting information), which display the weak interaction/bonding

**Table 3**

EDA results for  ${}^3\text{Nb}_3\text{N}_2^+$  and  ${}^1\text{Nb}_3\text{O}_2^+$  at the B3LYP/TZP level of theory using ADF, taking  $\text{Nb}_3^+$  and  $\text{N}_2$  ( $\text{O}_2$ ) as interacting fragments.  $\Delta E_{\text{int}}$  is the intrinsic interaction energies.  $\Delta E_{\text{pauli}}$  is the repulsion energy caused by the Pauli exclusion principle.  $\Delta E_{\text{ele}}$  and  $\Delta E_{\text{orb}}$  are the attraction energies due to electrostatic and orbital interactions, respectively. The values in parentheses show the contribution to  $\Delta E_{\text{int}}$  and the total orbital interaction  $\Delta E_{\text{orb}}$ .

${}^3\text{Nb}_3\text{N}_2^+$		${}^1\text{Nb}_3\text{O}_2^+$	
Energy term & assignment	kcal/mol	Energy term & assignment	kcal/mol
$\Delta E_{\text{int}}$	-13.6	$\Delta E_{\text{int}}$	-170.6
$\Delta E_{\text{pauli}}$	66.8	$\Delta E_{\text{pauli}}$	544.5
$\Delta E_{\text{ele}}$	-39.6 (49.2%)	$\Delta E_{\text{ele}}$	-287.1 (40.2%)
$\Delta E_{\text{orb}}$	-40.9 (50.8%)	$\Delta E_{\text{orb}}$	-430.0 (59.8%)
$\Delta E_{\text{orb-}\alpha(1)}$ : $\sigma$ donation + polarization	-10.3 (25.1%)	$\Delta E_{\text{orb-}\alpha(1)}$ : $\pi$ backdonation	-177.8 (41.5%)
$\Delta E_{\text{orb-}\alpha(2)}$ : $\pi$ backdonation	-4.1 (10.1%)	$\Delta E_{\text{orb-}\alpha(2)}$ : $\pi$ donation	-20.0 (4.7%)
$\Delta E_{\text{orb-}\alpha(3)}$ : polarization + $\pi$ backdonation	-3.0 (7.3%)	$\Delta E_{\text{orb-}\alpha(3)}$ : $\pi$ donation	-8.3 (1.9%)
$\Delta E_{\text{orb-}\beta(1)}$ : $\sigma$ donation + polarization	-9.5 (23.3%)	$\Delta E_{\text{orb-}\beta(1)}$ : $\pi$ backdonation	-177.8 (41.5%)
$\Delta E_{\text{orb-}\beta(2)}$ : $\pi$ backdonation	-5.8 (14.2%)	$\Delta E_{\text{orb-}\beta(2)}$ : $\pi$ donation	-20.0 (4.7%)
$\Delta E_{\text{orb-}\beta(3)}$ : $\pi$ backdonation	-3.2 (7.9%)	$\Delta E_{\text{orb-}\beta(3)}$ : $\pi$ donation	-8.3 (1.9%)
$\Delta E_{\text{orb}(4)}$ : rest	-5.0 (12.2%)	$\Delta E_{\text{orb}(4)}$ : rest	-16.0 (3.7%)



**Fig. 4.** Kohn–Sham orbital correlation diagrams of (a)  $\text{Nb}_3\text{N}_2^+$  in the triplet state. (b)  $\text{Nb}_3\text{O}_2^+$  in the stable triplet state. Blue lines are for orbitals composed by one part, and red lines are for orbitals interaction of two fragments with percentage which solid lines are for occupied orbitals and dotted line are for vacant orbitals. All the data are calculated at the B3LYP/TZP level of theory using ADF.

between  $\text{Nb}_3^+$  and  $\text{N}_2$ , while much larger donor-acceptor interaction energies for  $\text{Nb}_3\text{O}_2^+$  in the single state.

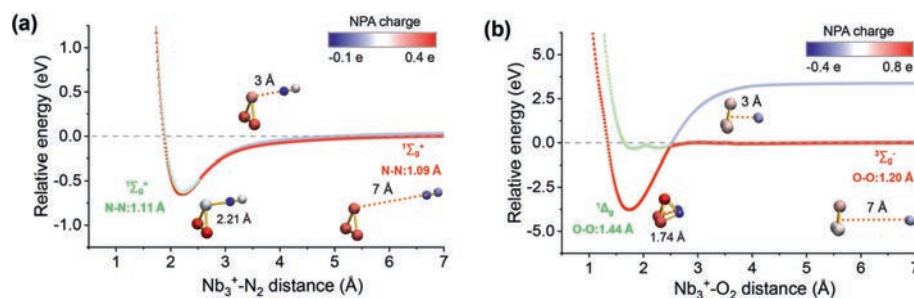
Figs. 5a and b present the potential scan curves of  $\text{Nb}_3^+$  in reacting with  $\text{N}_2$  and  $\text{O}_2$  respectively to form the products (more details of varying directions are given in Figs. S20 and S21 in Supporting information), where the NPA charge distribution is displayed in color with dependence on the varying distances of the reactants. For “ $\text{Nb}_3^+\cdots\text{N}_2$ ” (Fig. 5a), the two overlap curves display minor vibration of the N–N bond distance ranging from 1.09 Å to 1.11 Å. Considering that the product  ${}^1\text{Nb}_3\text{O}_2^+$  has an altered spin multiplicity and oxygen state comparing with the nascent  ${}^3\text{Nb}_3^+$  and  ${}^3\text{O}_2$ , we have performed the potential scan from two directions, allowing the geometrical configuration and spin multiplicity to be equal to the reactants and the products respectively. As is shown in Fig. 5b, the two scanning curves for “ $\text{Nb}_3^+\cdots\text{O}_2$ ” display a crossing at  $\sim 2.4$  Å, which indicates a critical value for the interaction distance of chemical reaction, and the energy minima point at a  $\text{Nb}_3^+\cdots\text{O}_2$  distance of 1.74 Å corresponds to the oxygen-activated state (i.e.,  ${}^1\Delta_g$  state, with O–O bond distance at 1.44 Å). Furthermore, Kohn–Sham orbital correlation diagrams, charge transfer diagrams along with orbital interactions and detailed NOCV analysis of  $\text{Nb}_3\text{O}_2^+$  in imaginary quintuplet state at a  $\text{Nb}_3^+\cdots\text{O}_2$  distance of 1.80 Å and O–

O bond distance of 1.20 Å are shown in Figs. S13, S15 and S19 in Supporting information).

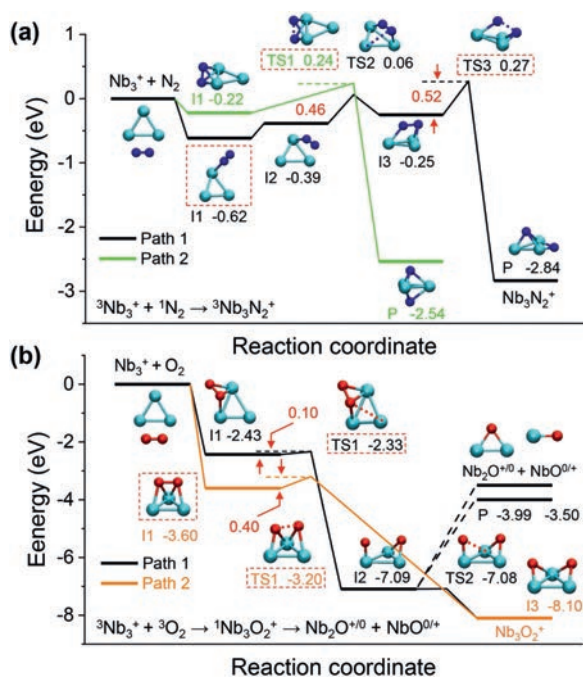
Having unveiled the different interactions involved in “ $\text{Nb}_3^+ + \text{N}_2$ ” and “ $\text{Nb}_3^+ + \text{O}_2$ ”, we then plotted the reaction coordinates for the reaction dynamics of the niobium clusters with oxygen and nitrogen, as shown in Fig. 6. Two reaction pathways are considered for  $\text{Nb}_3^+$  with  $\text{N}_2$  in view of the likely varying molecular orientation of dinitrogen in approaching the cluster. As is shown, when the dinitrogen takes an end-on adsorption on a vertex atom of the  $\text{Nb}_3^+$  cluster (black line), it gets a 0.62 eV energy gain but subsequent path toward the final dissociative  $\text{Nb}_3\text{N}_2^+$  needs to overcome a few endothermic steps and the rate-determine transition state TS3 is 0.27 eV higher than the relative energy of the reactants. Alternatively, if the dinitrogen molecule could approach the cluster via an orientation orthogonal to one of the triangular edges of the  $\text{Nb}_3^+$ , the reaction path (green line) needs to overcome a relatively smaller energy barrier but the rate-determine TS1 is still 0.24 eV higher in energy than the reactants. This energy barrier is small especially when considering the N≡N bond dissociation energy of  $\sim 9.79$  eV, but it could not proceed spontaneously in the thermalized flow tube reactors (where previous studies suggest a threshold value could be  $\sim 0.1$  eV by taking into consideration of vibrational, rotational and translational kinetic energy) [56,58].

In sharp contrast, the reaction of “ $\text{Nb}_3^+ + \text{O}_2$ ” is largely exothermic (8.10 eV in our calculation) to form an oxygen-dissociative products with two bridge oxygen atoms bonding to two edges of the triangular  $\text{Nb}_3^+$  cluster, and the spin multiplicity turns to be singlet indicative of spin accommodation in the reaction process of  ${}^3\text{Nb}_3^+$  with  ${}^3\text{O}_2$  [48,59]. Note that, this reaction to form oxygen-dissociated product is highly thermodynamic and also kinetics-favorable, with the TS1 being 2.33 eV (or 3.2 eV for the yellow line) lower than the total energy of the reactants. Therefore, the mass spectrometry observation of  $\text{Nb}_3\text{O}_2^+$  (and the other  $\text{Nb}_n\text{O}_2^+$ ) could be completely dissociated products. This is largely due to the large Nb–O bond energy ( $\sim 770$  kJ/mol) in contrast to the bond strengths of O–O ( $\sim 400$  kJ/mol) and Nb–Nb ( $\sim 513$  kJ/mol). The large amount of energy release by dissociative adsorption makes it feasible to produce odd-oxygen products (e.g.,  $\text{Nb}_2\text{O}^{+/0}$ ,  $\text{Nb}_n\text{O}_{1,3}^+$ ) along with the  $\text{NbO}^{0/+}$  removal.

In summary, utilizing our customized instrument MIFT-TQMS we report here an in-depth study to compare the gas-phase reactivity of  $\text{Nb}_n^+$  clusters with  $\text{N}_2$  and  $\text{O}_2$ . Under sufficient backing gas pressure (up to 1 Torr), the  $\text{Nb}_n^+$  clusters readily react with  $\text{N}_2$  and form a series of adsorption products  $\text{Nb}_n\text{N}_{2m}^+$ . In comparison, the  $\text{Nb}_n^+$  clusters react with  $\text{O}_2$  in a comparable rate but produce  $\text{Nb}_n\text{O}_{1-4}^+$  along with a rapidly growing product  $\text{NbO}^+$ , showing the O–O bond dissociation and metal cluster etching reactions akin to



**Fig. 5.** Potential scan curves of the  $\text{Nb}_3^+$  cluster in approaching (a)  $\text{N}_2$  and (b)  $\text{O}_2$  from two directions with the geometrical configuration and spin multiplicity equal to the reactants and the products respectively. Red lines refer to real approaching process due to energy crossing point, while light blue/green lines refer to imaginary scanning processes. The insets show the NPA charge of every atom as a function of different interaction distance.



**Fig. 6.** The calculated reaction pathways for (a) " $\text{Nb}_3^+ + \text{N}_2$ " and (b) " $\text{Nb}_3^+ + \text{O}_2$ ". All the thermodynamic data are calculated at the B3LYP/Lan12dz for Nb and B3LYP/6-311G (d) for O and N.

the previous findings on anionic aluminum and cobalt clusters. Energetics calculations show that the adsorption energies of  $\text{Nb}_n\text{O}_2^+$  (2.5–4 eV) are significantly larger than that of  $\text{Nb}_n\text{N}_2^+$  (0.5–0.9 eV). While the dinitrogen all follow an end-on orientation adsorption on the  $\text{Nb}_n^+$  clusters, the chemisorptive  $\text{Nb}_n\text{O}_2^+$  species conform to hollow-site adsorption along with spin-flip and perfect accommodation to be singlet. PDOS and frontier orbital analyses reveal strong  $\pi$  backdonation from  $\text{Nb}_n^+$  to  $\text{O}_2$ ; which is in contrast to the  $\text{Nb}_n\text{N}_2^+$  system which involves both  $\sigma$  donation from  $\text{N}_2$  to  $\text{Nb}_n^+$  and simultaneously weak  $\pi$  backdonation from  $\text{Nb}_n^+$  to  $\text{N}_2$ . Potential scan plots a van der Waals curve for the  $\text{N}_2$  molecule in approaching the  $\text{Nb}_3^+$  cluster, whereas the potential scan for " $\text{Nb}_3^+\cdots\text{O}_2$ " displays a crossing from two directions with the spin multiplicity equal to the reactants and the products respectively, shedding light on the spin crossing effect. Further, reaction dynamics calculation unveils feasible O–O bond dissociation and finally  $\text{NbO}$  ( $\text{NbO}^+$ ) removal from such  $\text{Nb}_n\text{O}_{2m}^+$  clusters.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Supplementary materials

Supplementary material associated with this article can be found, in the online version, at doi:10.1016/j.ccl.2021.04.020.

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